

# Asymptotically Better Query Optimization Using Indexed Algebra

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# Motivation

- Complex queries on small workloads
  - BigQuery: 90% of queries processed less than 100 MB of data
  - Tableau Public: 90% of workbooks are less than 100k tuples

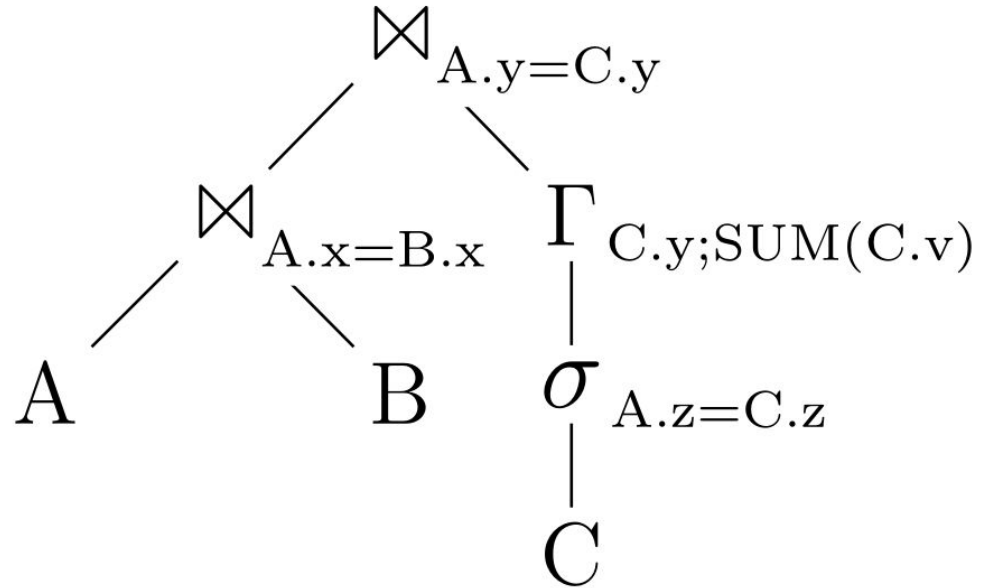
# Motivation

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  - BigQuery: 90% of queries processed less than 100 MB of data
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- TPC-H
  - Scale 1: 0.8 ms optimization, 20 ms execution
  - Scale 0.01: 0.8 ms optimization, 0.2 ms execution



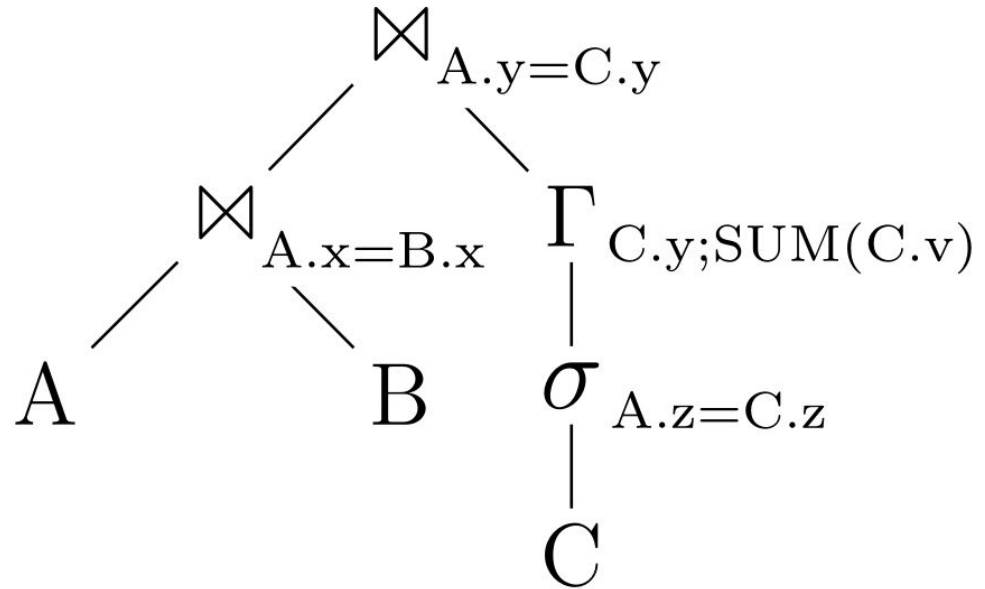
# Algebra

- Relational algebra trees
  - Operators
  - Expressions
  - Columns / IUs



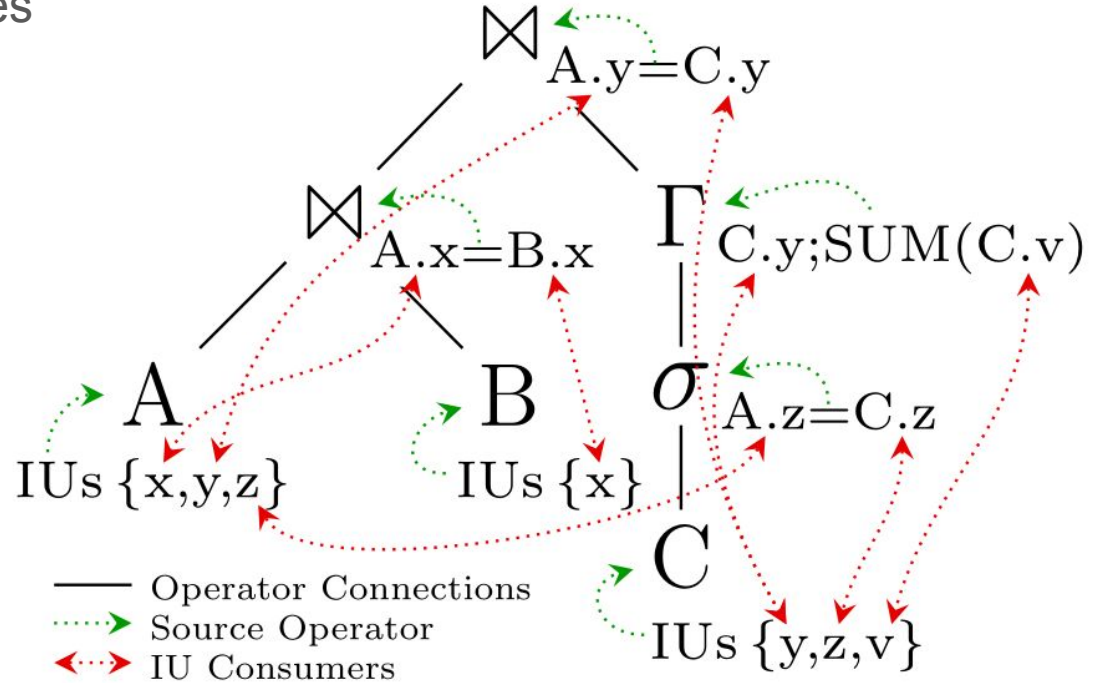
# Algebra

- Relational algebra trees
  - Operators
  - Expressions
  - Columns / IUs
- Analyze data-flow for optimization
  - Which path?
  - Modifications?
  - Materialized?



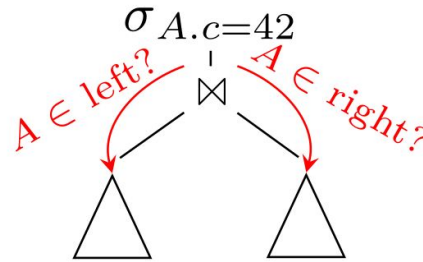
# Algebra

- Relational algebra trees
  - Operators
  - Expressions
  - Columns / IUs
- Analyze data-flow for optimization
  - Which path?
  - Modifications?
  - Materialized?
- Interconnected



# Optimization

- Reason about the algebra to derive optimization possibilities
- Top-down, operator at a time
  - Needs  $O(n^2)$  column sets

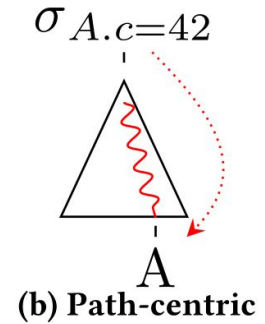
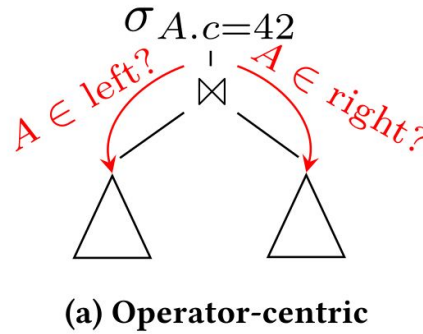


**(a) Operator-centric**



# Optimization

- Reason about the algebra to derive optimization possibilities
- Top-down, operator at a time
  - Needs  $O(n^2)$  column sets
- Path-centric
  - Still  $O(n)$  length
  - With indexing:  $O(\log n)$



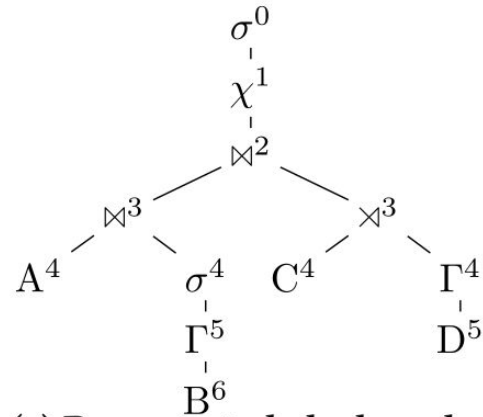
# Indexing Algebra

- Index paths through the algebra
  - ➔ Faster path traversal

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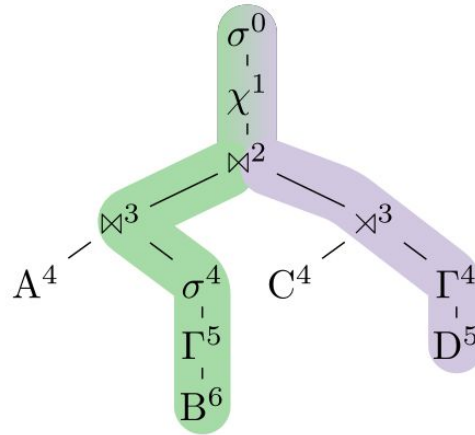
➔ Faster path traversal



**(a) Represented algebra plan**

# Indexing Algebra

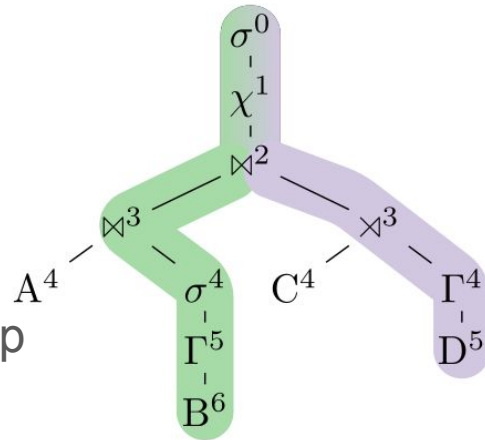
- Index paths through the algebra
  - ➔ Faster path traversal
- Binary search trees on path depth



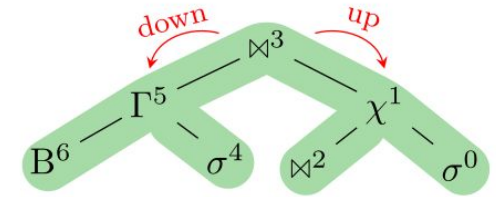
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# Indexing Algebra

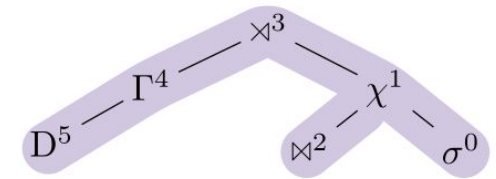
- Index paths through the algebra
  - ➔ Faster path traversal
- Binary search trees on path depth
- Paths from root might overlap



(a) Represented algebra plan



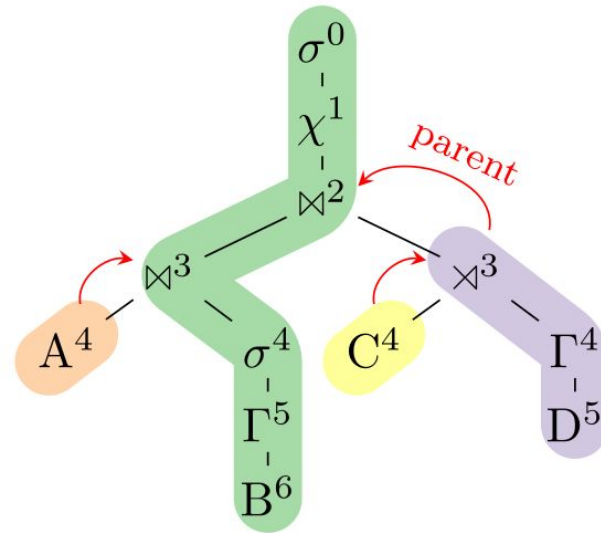
(b) Balanced binary index of the path from  $B^6$  to the root



(c) Index from  $D^5$  to the root

# Indexing Algebra

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- Binary search trees on path depth
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- **Link/cut trees** support that efficiently



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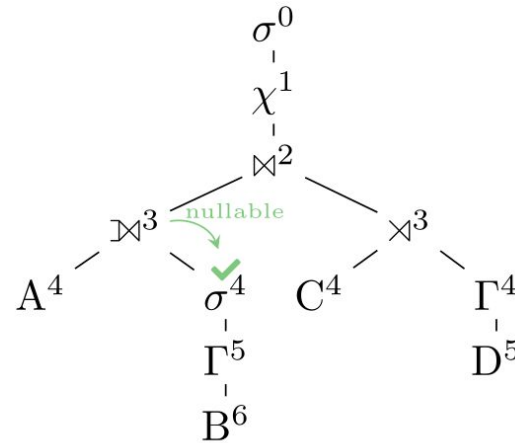
Rel. Algebra	Transformation	Traversal
w/o index	$O(1)$	$O(n)$
static index	$O(n)$	$O(\log n)$
path labeling	$O(n)$	$O(1)$
Indexed Algebra	$O(\log n)$	$O(\log n)$

# Path-centric optimization



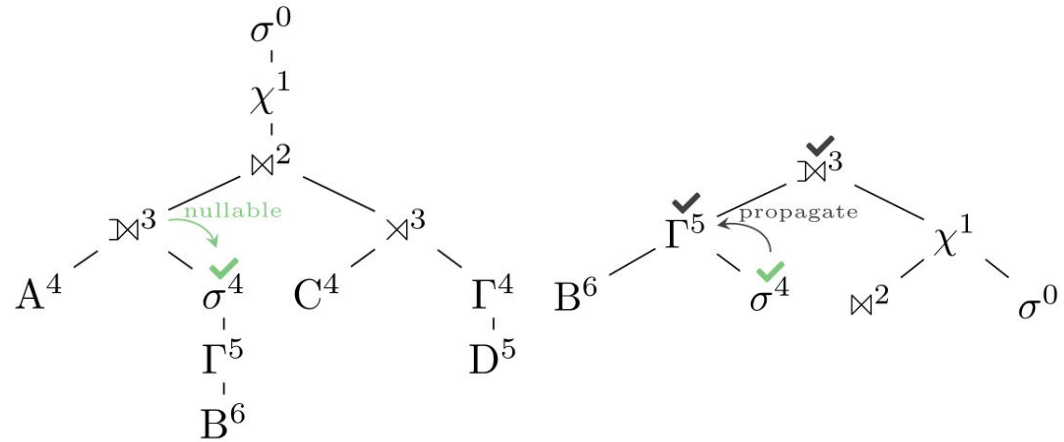
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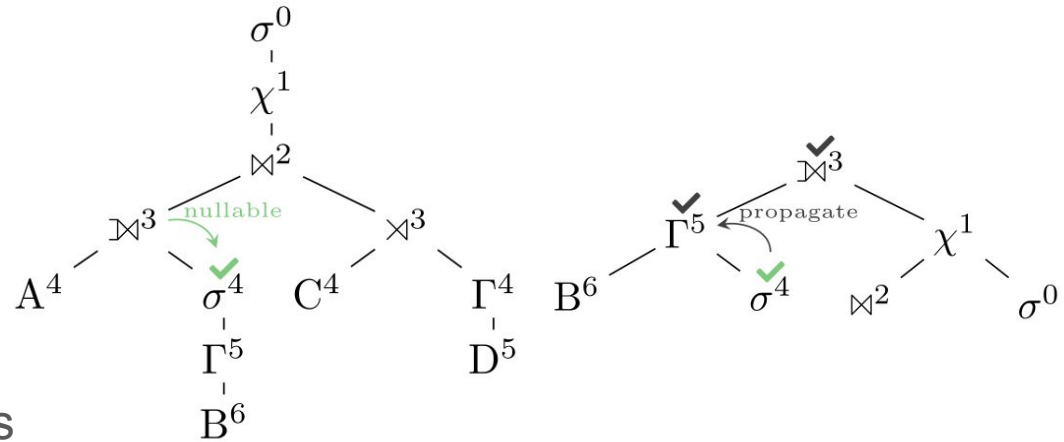


# Path-centric optimization

- Detect outer-joins on path
  - Mark children nullable
  - Propagate marker in index
- Check null bit in index
  - Cut away subtrees for partial path queries
- Predicate pushdown
 

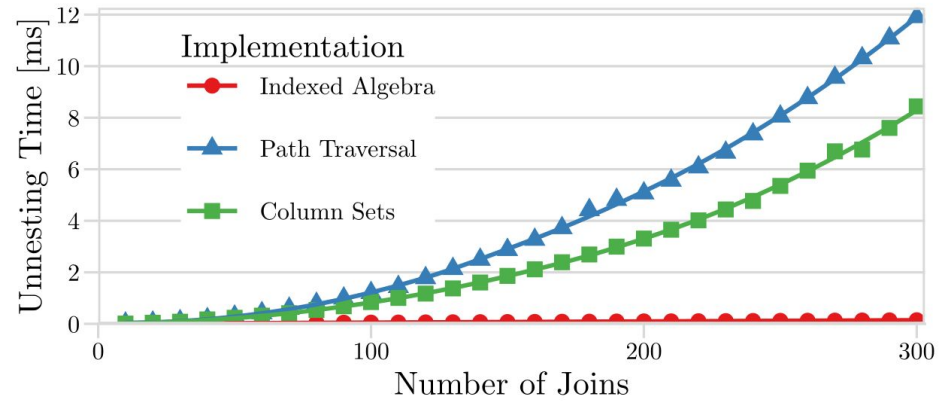
Constant propagation upwards

➔  $O(\log n)$



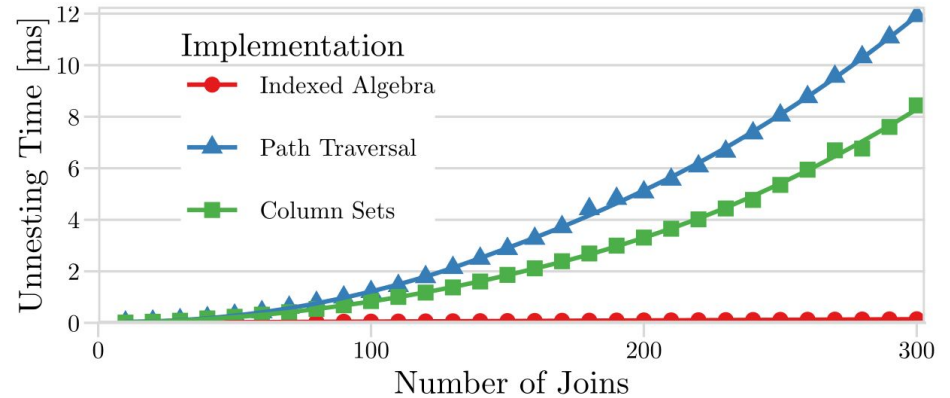
# Performance

- Clearly better asymptotics



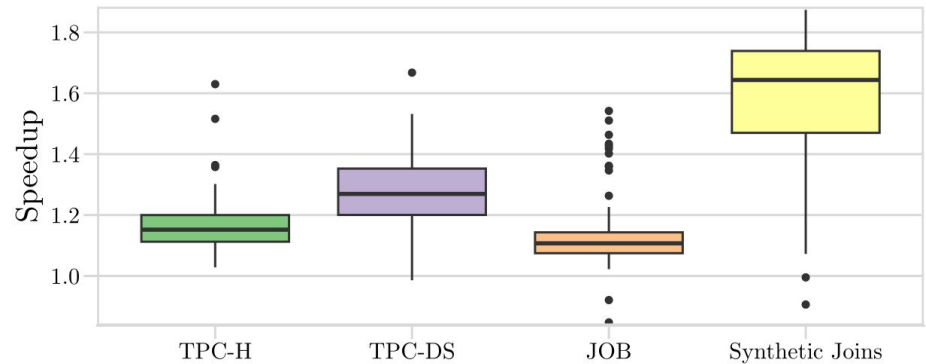
# Performance

- Clearly better asymptotics
  - Query unnesting is read-only
  - Path-labels would be even better but need  $O(n^2)$  construction



# Performance

- Significant overall improvements
- 10 - 30% faster optimization
- 8% better *end-to-end* latency in Tableau Public



# Asymptotically Better Query Optimization Using Indexed Algebra

- Asymptotically better query optimization
- Allows elegant and concise formulations for *data flow* questions
- But needs effort to reengineer the optimizer

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